

Bounding the Higgs Width Using Effective Field Theory*

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An interesting question is how present and future experiments will be able to probe the couplings of the Higgs boson and its intrinsic width at a high level of precision. There is a wide variety of beyond the Standard Model (BSM) theories where the Higgs couplings differ from the Standard Model (SM) ones by less than 10%. We take the SM as the theory of “light” degrees of freedom, i.e. $d = 4$ operators and simulate the unknown extension of the SM by the most general set of $d = 6$ operators. In particular we provide an explicit example of momentum-dependent modification of Higgs couplings.

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1. Introduction

Indirect constraints on the total Higgs width at LHC have received considerable attention and the CMS Collaboration [1] has presented the first measurement. The analysis is based on correlating the Higgs signal strength with measurements in the off-shell region. In Refs. [2, 3] the off-shell production cross section has been shown to be sizeable at high ZZ -invariant mass in the gluon fusion production mode, with a ratio relative to the on-peak cross section of the order of 8% at a center-of-mass energy of 8 TeV . This ratio can be enhanced up to about 20% when a kinematical selection used to extract the signal in the resonant region is taken into account [4]. This arises from the vicinity of the on-shell Z pair production threshold, and is further enhanced at the on-shell top pair production threshold.

In Refs. [5] the authors demonstrated that, with few assumptions and using events with pairs of Z particles, the high invariant mass tail can be used to constrain the Higgs width.

This note introduces the bases for a model-independent interpretation of the constraint, generalizing the arguments given in Ref. [6]; for complementary studies see Refs. [7, 8, 9].

2. On-shell ∞ -degeneracy

Refs. [10, 5, 11, 12] consider the following scenario (on-shell ∞ -degeneracy): allow for a scaling of the Higgs couplings (g_i, g_f) and of the total Higgs width (γ_H) defined by

$$\sigma_{i \rightarrow H \rightarrow f} = (\sigma \cdot \text{BR}) = \frac{\sigma_i^{\text{prod}} \Gamma_f}{\gamma_H}, \quad \sigma_{i \rightarrow H \rightarrow f} \propto \frac{g_i^2 g_f^2}{\gamma_H}, \quad g_{i,f} = \xi g_{i,f}^{\text{SM}}, \quad \gamma_H = \xi^4 \gamma_H^{\text{SM}}. \quad (2.1)$$

Looking for ξ -dependent effects in the highly off-shell region is an approach that raises sharp questions on the nature of the underlying extension of the SM; furthermore it does not take into account variations in the SM background and the signal strength in 4l, relative to the expectation for the SM Higgs boson, is measured by CMS to be $0.91_{-0.24}^{+0.30}$ [13] and by ATLAS to be $1.43_{-0.35}^{+0.40}$ [14]. We adopt the approach of Ref. [15] (in particular Eqs. (1-18)) which are based on the κ -language, allowing for a consistent ‘‘Higgs Effective Field Theory’’ (HEFT) interpretation, see Ref. [16]. For example, neglecting loop-induced vertices, in the production via gluon fusion we have:

$$\kappa_g^2 = \frac{\sigma_{ggH}(M_H)}{\sigma_{ggH}^{\text{SM}}(M_H)} = \frac{\kappa_t^2 \cdot \sigma_{ggH}^{\text{tt}}(M_H) + \kappa_b^2 \cdot \sigma_{ggH}^{\text{bb}}(M_H) + \kappa_t \kappa_b \cdot \sigma_{ggH}^{\text{tb}}(M_H)}{\sigma_{ggH}^{\text{tt}}(M_H) + \sigma_{ggH}^{\text{bb}}(M_H) + \sigma_{ggH}^{\text{tb}}(M_H)}. \quad (2.2)$$

The measure of off-shell effects can be interpreted as a constraint on γ_H only when we scale couplings and total width according to Eq.(2.1) to keep σ_{peak} untouched, although its value is known with 15–20% accuracy. The generalization of Eq.(2.1) is an ∞^2 -degeneracy, $\kappa_i \kappa_f = \kappa_H$, where $g_{i,f} = \kappa_{i,f} g_{i,f}^{\text{SM}}$, $\gamma_H = \kappa_H^2 \gamma_H^{\text{SM}}$.

On the whole, we have a constraint in the multidimensional κ -space of rescaling factors for couplings (for gluon fusion we have for instance, $\kappa_i = \kappa_g(\kappa_t, \kappa_b)$). Only on the assumption of degeneracy we can prove that off-shell effects ‘‘measure’’ κ_H ; a combination of on-shell effects (measuring $\kappa_i \kappa_f / \kappa_H$) and off-shell effects (measuring $\kappa_i \kappa_f$) gives information on κ_H without prejudices. Denoting by S the signal and by I the interference and assuming that I_{peak} is negligible we have

$$\frac{S_{\text{off}}}{S_{\text{peak}}} \kappa_H^2 + \frac{I_{\text{off}}}{S_{\text{peak}}} \frac{\kappa_H}{x_{if}}, \quad x_{if} = \frac{\kappa_i \kappa_f}{\kappa_H}, \quad (2.3)$$

for the normalized S + I off-shell cross section. The background, e.g. $gg \rightarrow 4l$, is also changed by the inclusion of $d = 6$ operators and one cannot claim that New Physics is modifying only the signal.

3. Higgs Effective Field Theory

CMS results raise a question: is there a QFT behind degeneracy with a consistent BSM interpretation? Our starting point is the following Lagrangian

$$\mathcal{L} = \mathcal{L}_4 + \sum_{n>4} \sum_{i=1}^{N_n} \frac{a_i^n}{\Lambda^{n-4}} \mathcal{O}_i^{(d=n)}, \quad (3.1)$$

where \mathcal{L}_4 is the Standard Model (SM) and Λ is a given cut-off. Any (pseudo-)observable starting at $\mathcal{O}(g^N)$ is given by

$$A = \sum_{n=N}^{\infty} \sum_{l=0}^n \sum_{k=1}^{\infty} g^n g_{4+2k}^l A_{nlk}, \quad g_{4+2k} = 1/(\sqrt{2} G_F \Lambda^2)^k, \quad (3.2)$$

where no hierarchy of higher-dimensional operators is assumed; for $\dim = 6$ operators we follow the work of Ref. [17] (for alternative approaches see Ref. [18] and also Ref. [19]). According to the work of Ref. [20] we distinguish between potentially-tree-generated (PTG) operators and loop-generated (LG) operators (an operator is PTG if it is generated in at least one extension of SM). It can be argued that (at LO) the basis operator should be chosen from among the PTG operators but it is also evident that one can take an $\mathcal{O}_{\text{LG}}^{(6)}$ and contract two lines forming a loop, which requires renormalization of some $\mathcal{O}^{(4)}$ and a SM vertex with $\mathcal{O}_{\text{PTG}}^{(6)}$ is also required. Furthermore, if we assume that the high-energy theory is weakly-coupled and renormalizable it follows that the PTG/LG classification of Ref. [20] (used here) is correct. If we do not assume the above but work always in some EFT context (i.e.. also the next high-energy theory is EFT, possibly involving some strongly interacting theory) then classification changes, see Eqs. (A1-A2) of Ref. [21]. Decoupling is also assumed, e.g. colored scalars disappear from the low energy physics as their mass increases but the same is not true for fermions.

Furthermore, we will not address the question of constraints on electroweak effective operators [7, 22, 8]; penalty functions can always be added in the fit.

Phrased differently, our questions are the following: are the $g_{i,f}$ factors in Eq.(2.1) constant or running? What is their relation with the κ -language once we extend it to next-to-leading (NLO) order? What is their relation with the Wilson coefficients of the relevant operators? What can we learn, in a model-independent way (although supporting a weakly-coupled and renormalizable UV completion), from off-shell cross section measurements?

Before we provide an answer we would like to stress that there are two ways of formulating an effective field theory [23]: a) mass-dependent scheme(s) or Wilsonian EFT, b) mass-independent scheme(s) or continuum EFT (CEFT). Only a) is conceptually consistent with the image of an EFT as a low-energy approximation to a high-energy theory, however inclusion of NLO corrections is only meaningful in b) since we cannot regularize with a cut-off and NLO requires regularization.

There is an additional problem, CEFT requires evolving our theory to lower scales until we get below the “heavy-mass” scale where we use $\mathcal{L} = \mathcal{L}_{\text{SM}} + d\mathcal{L}$, $d\mathcal{L}$ encoding matching corrections

at the boundary. Therefore, CEFT does not integrate out heavy degrees of freedom but removes them compensating for by an appropriate matching calculation. From this point of view HEFT is not quite the same as it is usually discussed since we have no theory approaching the boundary from above (cf. low-energy SM, weak effects on $g - 2$ etc.).

3.1 Renormalization

Once we have the Lagrangian of Eq.(3.1) the whole renormalization procedure (see Refs. [24, 25, 26]) must be reinitialized. Thus, part of the procedure consists of several steps:

- evaluation of tadpoles and introduction of counterterms, $\Phi = Z_\phi^{1/2} \Phi_R$ etc., where

$$Z_\phi = 1 + \frac{g^2}{16\pi^2} \left(\delta Z_\phi^{(4)} + g_6 \delta Z_\phi^{(6)} \right) \frac{1}{\bar{\epsilon}}; \quad (3.3)$$

- self-energies are computed and counterterms fixed to make them ultraviolet $\mathcal{O}^{(4)}$, $\mathcal{O}^{(6)}$ -finite;
- μ -decay is computed and coupling constant renormalization follows: $g \rightarrow g_R$;
- furthermore, finite renormalization is performed, e.g.

$$M_R^2 = M_W^2 \left[1 + \frac{g_R^2}{16\pi^2} (\text{Re } \Sigma_{WW} - \delta Z_M) \right], \quad \text{etc.}; \quad (3.4)$$

- Dyson re-summed propagators are finite; for instance

$$\begin{aligned} \Delta_H^{-1} &= Z_H \left(-s + Z_{m_H} M_H^2 \right) - \frac{1}{(2\pi)^4 i} \Sigma_{HH}, \\ m_H^2 &= M_H^2 \left[1 + \frac{g_R^2}{16\pi^2} \left(dM_H^{(4)} + g_6 dM_H^{(6)} \right) \right], \end{aligned} \quad (3.5)$$

where m_H is the renormalized Higgs mass and M_H is the on-shell mass (in this note we are not going to discuss/introduce complex poles).

3.2 Effective couplings

Consider off-shell gluon-gluon fusion ($gg \rightarrow H$, where v_H is the Higgs virtuality): it requires the introduction of renormalization factors Z_H , Z_g for the external fields, Z_g for the $SU(2)$ coupling and Z_{g_s} for the strong coupling constant. The amplitude is obviously $\mathcal{O}^{(4)}$ -finite but not $\mathcal{O}^{(6)}$ -finite and involves the following Wilson coefficients (see Ref. [17]): $a_{\phi D}$, $a_{\phi \square}$, $a_{t\phi}$, $a_{b\phi}$ for PTG operators and $a_{\phi W}$, $a_{\phi g}$, a_{tg} , a_{bg} for LG operators. It is convenient to introduce

$$\begin{aligned} a_{tg} &= W_1, & a_{bg} &= W_2, & a_{\phi g} &= W_3, \\ a_{b\phi} + \frac{1}{4} a_{\phi D} - a_{\phi W} - a_{\phi \square} &= W_4, & a_{t\phi} - \frac{1}{4} a_{\phi D} + a_{\phi W} + a_{\phi \square} &= W_5. \end{aligned} \quad (3.6)$$

$\mathcal{O}^{(6)}$ -finiteness requires extra renormalization, i.e.

$$W_i = \sum_j Z_{ij}^{\text{mix}} W_j^R(\mu_R), \quad Z_{ij}^{\text{mix}} = \delta_{ij} + \frac{g g_s}{16\pi^2} \delta Z_{ij}^{\text{mix}} \frac{1}{\bar{\epsilon}}, \quad \delta Z_{31(2)}^{\text{mix}} = -\frac{1}{2\sqrt{2}} \frac{M_{t(b)}}{M_W}. \quad (3.7)$$

We define building blocks using $B_0(C_0)$ for the scalar two(three)-point function

$$\frac{8\pi^2}{i g_S^2} \frac{M_W}{M_q^2} A_q^{\text{LO}} = 2 - \left(4M_q^2 - v_H\right) C_0(-v_H, 0, 0; M_q, M_q, M_q), \quad (3.8)$$

$$\frac{32\pi^2}{i g_S^2} \frac{M_W^2}{M_q} A_q^{\text{nfc}} = 8M_q^4 C_0(-v_H, 0, 0; M_q, M_q, M_q) + v_H \left[1 - B_0(-v_H; M_q, M_q)\right] - 4M_q^2, \quad (3.9)$$

and process dependent κ -factors (which are now linear combinations of Wilson coefficients)

$$\kappa_b = 1 + g_6 \left[\frac{1}{2} \frac{M_b}{M_W} W_2^{\text{R}} - \frac{1}{\sqrt{2}} W_4^{\text{R}} \right], \quad \kappa_t = 1 + g_6 \left[\frac{1}{2} \frac{M_t}{M_W} W_1^{\text{R}} - \frac{1}{\sqrt{2}} W_5^{\text{R}} \right]. \quad (3.10)$$

With their help we construct the full 4+6 amplitude for $gg \rightarrow H$,

$$A_{gg \rightarrow H}^{(4+6)} = g \sum_{q=b,t} \kappa_q A_q^{\text{LO}} + i \frac{g_6 g_S}{\sqrt{2}} \frac{M_H^2}{M_W} W_3^{\text{R}} + g_6 g \left[W_1^{\text{R}} A_t^{\text{nfc}} + W_2^{\text{R}} A_b^{\text{nfc}} \right], \quad (3.11)$$

and derive a true relation expressing deviations from the SM and momentum-dependent modification of Higgs couplings,

$$A^{(4+6)}(gg \rightarrow H) = \xi_g(v_H) A^{(4)}(gg \rightarrow H). \quad (3.12)$$

Therefore, the answer to the question on the nature of the couplings in Eq.(2.1) is that the effective (running) scaling-factor ξ_i is not a κ (constant) parameter unless we put $\mathcal{O}_{\text{LG}}^{(6)} = 0$ and $\kappa_b = \kappa_t$.

3.3 Scale dependence

The (μ_R) scale dependence of the full amplitude (from the point of view of renormalization group evolution of the SM $\text{dim} = 6$ operators see also Refs. [27, 28, 29, 30]) follows from the fact that we have no matching condition. Therefore the mixing among Wilson coefficients should be rewritten as

$$\begin{aligned} W_i &= \sum_j Z_{ij}^{\text{mix}} W_j^{\text{R}}(\mu_R), \quad W_1 = a_{\gamma\gamma} = s_\theta c_\theta a_{\Phi WB} + c_\theta^2 a_{\Phi B} + s_\theta^2 a_{\Phi W}, \quad \text{etc.} \\ Z_{ij}^{\text{mix}} &= \delta_{ij} + \frac{g_R^2}{16\pi^2} \left[\delta Z_{ij}^{\text{mix}} \frac{1}{\bar{\epsilon}} + \Delta_{ij} \ln \frac{M_H^2}{\mu_R^2} \right], \\ M_W^2 \Delta_{11} &= \frac{1}{4} \left[8s_\theta^2 (2s_\theta^2 - c_\theta^2) M_W^2 + (4s_\theta^2 c_\theta^2 - 5) M_H^2 \right], \quad \text{etc.} \end{aligned} \quad (3.13)$$

Here $c_\theta^2 = M_W^2/M_Z^2$. In the $\overline{\text{MS}}$ scheme this defines μ_R -dependent renormalized coefficients. The life and death of μ_R can be summarized as follows: consider the γ bare propagator

$$\begin{aligned} \Delta_\gamma^{-1} &= -s - \frac{g^2}{16\pi^2} \Sigma_{\gamma\gamma}(s), \quad \{\mathcal{X}\} = \{s, m^2, m_0^2, m_H^2, m_t^2, m_b^2\}, \\ \Sigma_{\gamma\gamma}(s) &= \left(D^{(4)} + g_6 D^{(6)} \right) \frac{1}{\bar{\epsilon}} + \sum_{x \in \mathcal{X}} \left(L_x^{(4)} + g_6 L_x^{(6)} \right) \ln \frac{x}{\mu_R^2} + \Sigma_{\gamma\gamma}^{\text{rest}}. \end{aligned} \quad (3.14)$$

Build the γ renormalized propagator

$$\Delta_\gamma^{-1} \Big|_{\text{ren}} = -Z_\gamma s - \frac{g^2}{16\pi^2} \Sigma_{\gamma\gamma}(s) = -s - \frac{g^2}{16\pi^2} \Sigma_{\gamma\gamma}^{\text{ren}}(s), \quad (3.15)$$

and the renormalized γ self-energy

$$\Sigma_{\gamma\gamma}^{\text{ren}}(s) = \sum_{x \in \mathcal{X}} \left(L_x^{(4)} + g_6 L_x^{(6)} \right) \ln \frac{x}{\mu_R^2} + \Sigma_{\gamma\gamma}^{\text{rest}}. \quad (3.16)$$

After finite renormalization we obtain

$$\Sigma_{\gamma\gamma}^{\text{ren}}(s) = \Pi_{\gamma\gamma}^{\text{ren}}(s) s, \quad \frac{\partial}{\partial \mu_R} \left[\Pi_{\gamma\gamma}^{\text{ren}}(s) - \Pi_{\gamma\gamma}^{\text{ren}}(0) \right] = 0, \quad (3.17)$$

including $\mathcal{O}^{(6)}$ contribution. Thus, there is no μ_R -problem when a subtraction point is available (e.g. $q^2 = 0$ for the electric charge).

3.4 Complexity and Background

The example of $gg \rightarrow H$ is particularly simple but there is an increasing degree of complexity when we move to other processes. For instance, for $H \rightarrow \gamma\gamma$ we have 3 LO amplitudes ($A_t^{\text{LO}}, A_b^{\text{LO}}, A_W^{\text{LO}}$), 3 κ -factors and 6 Wilson coefficients & non-factorizable amplitudes. For $H \rightarrow ZZ$ there is 1 LO amplitude, 6 NLO amplitudes, 6 κ -factors

$$\delta^{\mu\nu} \sum_{i=t,b,B} A_{i,D}^{\text{NLO}} + p_2^\mu p_1^\nu \sum_{i=t,b,B} A_{i,P}^{\text{NLO}}, \quad (3.18)$$

and 16 Wilson coefficients & non-factorizable amplitudes, etc..

Finally, we consider the background, e.g. $\bar{u}u \rightarrow ZZ$. The following combinations of Wilson coefficients appear:

$$\begin{aligned} (\text{LG}) \quad W_1 &= a_{\gamma\gamma} = s_\theta c_\theta a_{\Phi WB} + c_\theta^2 a_{\Phi B} + s_\theta^2 a_{\Phi W}, \\ (\text{LG}) \quad W_2 &= a_{ZZ} = -s_\theta c_\theta a_{\Phi WB} + s_\theta^2 a_{\Phi B} + c_\theta^2 a_{\Phi W}, \\ (\text{LG}) \quad W_3 &= a_{\gamma Z} = 2s_\theta c_\theta (a_{\Phi W} - a_{\Phi B}) + (c_\theta^2 - s_\theta^2) a_{\Phi WB}, \\ (\text{PTG}) \quad W_4 &= a_{\Phi D}, \quad W_5 = a_{\Phi q}^{(3)} + a_{\Phi q}^{(1)} - a_{\Phi u}, \quad W_6 = a_{\Phi q}^{(3)} + a_{\Phi q}^{(1)} + a_{\Phi u}. \end{aligned} \quad (3.19)$$

Defining the kinematical part of the LO amplitude as

$$A^{\text{LO}} = \frac{M_Z^4}{t^2} + \frac{M_Z^4}{u^2} - \frac{t}{u} - \frac{u}{t} - 4 \frac{M_Z^2 s}{tu}, \quad (3.20)$$

we obtain the result ($\bar{u}u \rightarrow ZZ$)

$$\sum_{\text{spin}} \left| A^{(4+6)} \right|^2 = g^4 A^{\text{LO}} \left[F^{\text{LO}}(s_\theta) + \frac{g_6}{\sqrt{2}} \sum_{i=1}^6 F^i(s_\theta) W_i \right]. \quad (3.21)$$

4. Conclusions

Thanks to the work of different groups we know that a combination of on-shell effects and off-shell effects gives information on the Higgs boson intrinsic width. Interpretation of the measurements and possible signals for deviations from the SM cannot live without an underlying theory. We have shown that, within a model-independent NLO approach, the Higgs couplings must

be interpreted as “running” couplings, expressible as linear combinations of Wilson coefficients of higher-dimensional operators and including non-factorizable components. Consequently any measurement of the couplings can be interpreted as a measure of the Wilson coefficients. Assuming that LHC will reach the needed sensitivity, this information will be a (blurred) arrow in the space of BSM Lagrangians, and we should simply focus the arrow.

It is worth noting that this question is highly difficult to receive a complete answer at the LHC. The main goal will be to identify the structure of the effective Lagrangian and to derive qualitative information on new physics; the question of the ultraviolet completion cannot be answered unless there is sensitivity to $d > 6$ operators. Therefore, we are proposing a relatively modest goal on the road to understand if the effective theory can be UV completed (bottom-up approach with no obvious embedding).

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